The Impact on World Population Growth of Possible Delays in the Decline in Fertility - Alternative Population Projections to Those of the United Nations

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Paper presented to the 13th World Congress of Sociology, Symposium V: The Environment, Technology, and Power, Session 2 - Population, Environment and Sustainable Livelihood

held at the University of Bielefeld, Germany on July 20, 1994

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Bielefeld, July 1994

Foreword

The population projections presented in this paper were produced as part of a research project currently being conducted, with financial support from the German World Population Foundation (Deutsche Stiftung Weltbevölkerung), at the University of Bielefeld's Institute for Population Research and Social Policy. The empirical computations were made by Carsten Wessel, an academic assistant at the Institute. A comprehensive research report will be published shortly in book form.

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1. Introduction and Proposition

Public interest in the issue of world population growth is largely concentrated upon the double question of how long the population will continue to grow (i.e., up to which year) and what level it will have reached by that time, likely to be in the late 21st or early 22nd century. As long as the number of live births per woman, defined as the total fertility rate (TFR), remains above 2.13 (the replacement fertility level) on a world average, the population will go on increasing. Because of the relatively young profile of the world population, even after the replacement fertility level has been attained and subsequently maintained, it will in fact still go on growing for between 50 and 100 years more. The crucial question is therefore how many decades will be needed before the total fertility rate comes down to the replacement fertility level of 2.13 live births per woman.

The present-day total fertility rate is 1.91 in the industrial countries, 3.64 in the developing countries, and 3.26 for the world as a whole. If the two separate rates for the industrial and developing countries were each to continue unchanged the effect on the world average total fertility rate would be for it to rise rather than fall as projections assume: for example, by the year 2050 it would have risen to 3.39 from the current 3.26. In view of the indisputable rise in the developing countries' share of total world population, it is fair to ask how probable it is that the world's total fertility rate really will have come down to replacement level by the year 2060 as assumed, for example, by the World Bank in its latest estimates. That question will be addressed in this paper. To aid the assessment, the conclusions of the current world population projections issued by the World Bank (1) and the United Nations Population Division (2) will be presented and compared with the projections made by the University of Bielefeld Institute of Population Research and Social Policy (3) with the support of the German World Population Foundation (Deutsche Stiftung Weltbevölkerung).

Over the past few decades, the average total fertility rate for the world population as a whole has fallen considerably, from 4.90 live births per woman in the 1960-65 period to 3.26 in 1990-95. This pronounced absolute drop has diverted attention from the fact that the actual pace of the decline has slowed steadily during those three decades. Indeed, if the high rate of decline between 1965-70 and 1975-80 had been maintained, the total fertility rate (2.13 live births per woman) ought already to have reached replacement level between 1993 and 1994. In reality though, the total fertility rate in 1993/94 was not 2.13 but, as already stated, 3.26 live births per woman. A number of statistics help to illustrate how much the pace of decline has slowed: between the

second half of the 1960s and the second half of the 1970s, the TFR fell by 1.05 live births per woman; between the second half of the 1970s and the second of the 1980s, the corresponding fall was less than half of that, at only 0.41 live births per woman (1975-80: 3.84; 1985-90: 3.43). The proposition which will be put forward in this paper is that the pace of decline in the total fertility rate is likely to continue slackening in the decades ahead. The proposition is not based simply on a projection of earlier trends, but on the following three substantive arguments:

- 1. People in the developing countries are likely to realize that, given the inadequacy of state unemployment and sickness benefits and old-age pensions, two children who attain adult age will not be sufficient to safeguard their parents' economic livelihood, to maintain family networks of mutual assistance or to comply with religious commandments and cultural norms.
- 2. Because of this, it will be all the more difficult to achieve further reductions in the level of fertility the lower that level has already sunk. In order to reduce the number of children per woman by the same amount each decade, ever greater efforts will be called for on the part of development, population and family planning policies. That in turn will mean that so many funds will be required that donor countries will have to substantially increase the assistance they provide.
- 3. As their relative demographic weighting increases, the developing countries' contribution towards the world total fertility rate will also steadily increase, so that a growing proportion of development and population policy efforts will need to be devoted even just to counterbalancing the increase in world total fertility rate caused by that change in weighting alone.

These propositions do not contradict the findings of the Demographic and Health Surveys (DHS) or the Family Planning Surveys (FPS) conducted by Johns Hopkins University in 40 developing countries during the 1980s (4). When the results of these were published in December 1992, the figures were misunderstood all around the world as implying that the situation was now easing (5). Yet demographic researchers see no reason at present to revise any earlier population projections downwards - quite the reverse. The UN's Population Division did not make any adjustments at all to its 1990 assumptions when making its latest estimates of the future trend in the total fertility rate in developing countries, while the latest publication on the subject by the World Bank (1992-93) actually revised the forecast TFR slightly upwards for the second half of the 21st century.

2. <u>Methodological Aspects, Basic Terms and the Initial Data used for Population Projections</u>

2.1 <u>Initial Population, Fertility, Mortality and Projection Method</u>

The population projections presented with this paper have been prepared using the same method as those published by the World Bank and the UN Population Division, namely what is known as the cohort survival method. So as to be able to delineate as clearly as possible between the influence of the age profile and that of fertility and mortality rates on the final results obtained, the base population in 1990 was differentiated by 100 different years of age and by gender (6). Taking 1990 as the base year, the next step is to calculate the number of males and females in each age cohort who are expected to survive into the following year, according to the statistical survival probability for the gender and age-group. When that operation is complete, one year is added to the age of each of the 200 cohorts, and the same procedure is then repeated for the surviving 1991 population thus obtained, and for each subsequent year until the end of the projection period is reached. Hence a projection running until the year 2100 which has 1990 as its base year will call for 110 computational steps, and the number of people surviving into, say, 2050 will be calculated on the basis of the projected population in 2049. The survival probabilities for the world population needed to apply this method were computed separately for each age cohort and each gender. The parameters used also took account of the fact that the survival probabilities of younger people are rising considerably faster than those of older age-groups in the population.

The number of live-born children in any given year of the projection period less the figure deducted for infants dying before they reach one year of age gives the world population in the 0—1 age-group for the start of the following year. The method used to calculate the number of live-born children each year is as follows: First the number of women in each of the 31 age cohorts (15-45) who have survived until that year in the projection is identified from the calculations already made. Then the number of women in each of those cohorts is multiplied by the corresponding age-specific fertility rate (of which there are again 31 different rates), and the aggregate number of live births for the year is established by adding all of the age-specific results together. The age-specific fertility rate is nothing more than the probability that a woman in a particular age-group will give birth to a child during the following year. Starting out

at a very low value at age 15, the age-specific fertility rates are distributed along a bell-shaped curve which returns to zero around the age of 45 years. The age-specific fertility rates all add together to give the total fertility rate.

2.2 Replacement Fertility Level

The replacement fertility level is the particular total fertility rate which, at a predetermined mortality level (derived from the measure of survival probabilities), allows just enough children to be born to replace their parents' generation. On the basis of the present and future life expectancies which have been used and assumed for these projections, that replacement fertility rate is 2.13 live births per woman. In other words, every 100 women need to give birth to 213 children for the population to sustain itself in the long run.

However, even assuming that the world's total fertility rate, at some point in the future, were to reach the replacement fertility level, the population itself would continue to grow for a further 50 to 100 years because of the *demographic momentum* inherent in the relatively young age profile, before it attained a stationary state in which both the total population figure and the age profile remained stable.

In such a stationary state, the *net reproduction rate* (NRR) equals 1. The net reproduction rate is the ratio of the size of a new generation relative to its parents' generation. As a general rule, if the NRR is greater than one (>1), the population will grow, if NRR<1 it will fall, and if it equals 1, it will remain constant. To illustrate, the net reproduction rate in the reunified Germany is currently 0.64, at which the population, were it not for the net immigration into the country, would decline by about 36% from one generation to another (in approx. 28 years).

The methods of demographic projection allow a precise answer to be given to the following hypothetical question: Assuming the total fertility rate were to come down to the replacement fertility level of 2.13 live births per woman in just one year, by how many people, or by what percentage, would the world population continue to grow? And that answer is that the world population would grow from 5.3 billion in 1990 to 7.3 billion in 2040, or in other words by approx. 40%! The significance of this hypothetical calculation is that it clearly demonstrates the importance of attaining replacement fertility as early as possible. If it were not attained in one year as in the hypothetical case just cited, but in an equally hypothetical period of 10 years, the world

population would than go on growing until the year 2050, and would stabilize at the higher level of 7.9 billion. Such computations will be illustrated in more detail and on a systematic basis below.

The computations shown here should <u>not</u> be regarded as *population forecasts or prophecies*; rather they consist of "if ... then ..." statements with regard to the future. That is to say, these statements as to future developments will prove true if the assumptions on which they are based are fulfilled. The consequences for fertility and mortality derived from these if-then conditions can be ascertained with a high degree of accuracy.

3. Impact of Alternative Fertility Scenarios on World Population Growth

3.1 Alternative Patterns of Decline and Target Years for Fertility Reduction (= Fertility Paths)

The target year is the description given to the future year at which the world total fertility rate is expected to have fallen from the 3.4 live births per woman registered in the base year (1990) to the replacement fertility level of 2.13 live births per woman. The alternative target-year scenarios reflect varying degrees of optimism in the assumed rapidity with which fertility will decline in future. As has been pointed out, these are *not* forecast values, but alternative sets of if-then assumptions, and the current purpose is to investigate the consequences flowing from particular assumptions of this kind. As there is no special need here to examine particular target years, an interval of 10 years has been chosen, giving the sequence of 2000, 2010, 2020, ..., 2060 (i.e. the target year assumed in the World Bank's projections), 2070, ..., 2100. It would be equally possible to make the calculations for any other target year in between. Of course, each specific target year gives rise to its own variant projection of world population growth.

In addition to the target year for the reduction in fertility, it is also necessary to establish what form that reduction should take, i.e. what the pattern of decline might be. The proposition made in section 1 above, that as fertility goes on falling it will become increasingly difficult to achieve any further decline, is best reflected in the assumption that the fertility curve will take the shape of a concave hyperbola. As alternatives to the hyperbolic curve, calculations have also been carried out on the assumption that the fall in fertility describes an S-curve (with the fastest rate of decline in the middle of the period and slower initial and final rates of decline) and finally also assuming a linear reduction (see Graphs 2—6). Hence three different population projections have been computed for each of the target years selected, as follows:

Pattern of decline in fertility

Target year for attaining replacement fertility level

- Hyperbolic
- S-curve

Linear

2000, 2010, ..., 2060, ..., 2100, ...

Each combination of a particular target year and a particular pattern of decline gives rise to its own path of fertility decline over time (or "fertility path" for short) and to a corresponding population projection.

3.2 <u>Population Projections for Alternative Fertility Paths and the Differences</u> between Global and Country-Specific Population Projections (Aggregation Effects)

For the "medium variant" of the World Bank's population projections, 2060 was chosen as the target year. When that same target year is chosen here, along with other alternative target years, the fertility paths arising from the three different types of decline produce the projections set out in Table 1. The population figure for the year 2150 emerging from the World Bank's projection is 12.1 billion, whereas the figure produced by the projections discussed here, on the lower variant, is just 10.7 billion. How does such a wide discrepancy arise? To examine one possibility, the hyperbolic time path chosen here is compared with the World Bank's assumption on the decline of fertility in Graph 6. Readers will notice that the hyperbolic curve runs above the World Bank's assumed fertility curve from 2035 onwards. If anything, then, one would expect a higher projection than the World Bank's to result, and not a lower one.

The reason for this discrepancy is what is known as the aggregation effect, the essence of which will be illustrated below. The population projections made by the World Bank and by the UN Population Division are based on separate computations for more than 150 countries around the world, which are subsequently added together to obtain the world total. This approach is known as a disaggregated projection. By way of contrast, the projections under discussion have been prepared on an aggregated world basis from the outset. One might at first think that the aggregated and disaggregated projections would be identical in their outcomes provided that they used the same base data and that all the underlying fertility and mortality assumptions were the same. However, that is not the case, as will be demonstrated by the following example.

Suppose we prepare one population projection for the world as a whole on an aggregate basis, and that we then make a second projection in which the world population is subdivided into two large parts, one for the industrial and one for the developing countries (a disaggregated projection). In the latter case, the projection for the world as a whole is obtained by adding together the two sub-populations for the industrial countries and the developing countries. Suppose also that we apply the same

assumptions on future fertility trends to both the aggregated and disaggregated projections. For the sake of simplicity, we may take a constant total fertility rate both in the industrial and in the developing countries, but with the latter higher than the former. Now, if we similarly assume a constant total fertility rate for the aggregated projection, this is where the discrepancy arises, for in the case of the disaggregated computation method the assumption of constant fertility in each sub-group would actually imply an increase in the world total fertility rate over time, since it is calculated as the weighted average of the specific fertility rates in the industrial countries on the one hand and the developing countries on the other. Provided that the TFR in each of the two sub-groups remains constant, that weighted average will inevitably increase because the developing countries with their higher specific fertility rate will take up an increasing relative share of the world population while the relative share of the industrial countries, with their lower fertility rate, declines. Thus precisely because we have supposed that the TFRs are constant in both the developing countries and the industrial countries, it is impossible for the world TFR to remain constant in the disaggregated projection method - it must inevitably increase. Conversely, one can conclude that if the world fertility path of a disaggregated population projection derived from specific country figures is the same as the fertility path underlying an aggregated world population projection, then the fertility assumptions made must have been different. As will be seen from Graph 6, the fertility paths for the target year of 2060 in the projection presented here and for the World Bank's projection are broadly the same, which means that the underlying fertility assumptions must be different, with a lower assumed fertility in this study than in the World Bank projection with the same target year. Consequently, the projected eventual population figure is also lower, since both projections work with the same base population and with largely identical mortality assumptions (7). From these considerations, we can conclude that it will be necessary to select a higher fertility path if we wish to compare the population projections presented here with those of the World Bank and the UN Population Division. The comparison can readily be made if a higher fertility path is chosen instead of the path with 2060 as the target year. The figures in Table 1 show that the hyperbolic fertility path with a target year in the 2080-85 range would fit such a comparison: by shifting the target 20-25 years further forward in time to 2080-85, we obtain a fertility path equivalent to that of the World Bank's projection, and the resulting projected population figures are in the same order of magnitude.

Another possible way of attaining comparability between aggregated and disaggregated population projections is to choose an S—curve or linear decline in fertility instead of

the hyperbolic curve, as the resulting fertility level is invariably higher in either of these alternative cases for any given target year. However, the fertility with a target year of 2060 then turns out higher than in the World Bank's projection: the linear fertility path produces a projected population in 2150 of 13.9 billion, and the S—curve path a projection of 13.7 billion. The population level projected by the World Bank is now arrived at by bringing the target closer in time, to the years 2045-50 for the linear option or 2040-45 for the S—curve option.

Table 1 and Graphs 7-9 show the resulting aggregated population projections for various alternative target years and patterns of fertility decline. The following important findings should be particularly pointed out:

- 1. Given a medium mortality trend and a replacement fertility level of 2.13, choosing which pattern of fertility reduction to assume results in a discrepancy, taking the target year of 2060 as an example, of approximately 3 billion in the final population figure projected. If the target year chosen is 2070, that discrepancy widens to 4billion, and if it is 2080, to 5billion. Even if the relatively close target year of 2030 is chosen, there is still a discrepancy in the final total of 1.2 billion.
- 2. The results obtained using S-curve and linear fertility paths are quite similar, and the final population projections they give when the target year for replacement fertility is 2060 lie approximately 30% above the final level obtained when a hyperbolic fertility path is assumed.

To sum up, not only the target year for replacement fertility and the replacement level itself are significant, but the actual pattern of fertility decline is an important factor in population growth in its own right, and the latter has received too little attention to date.

3.3 Path Effects

In *Graph 10a*, a linear fertility path with 2060 as the target year (curve "C") is superimposed on a hyperbolic curve with 2080 as the target year (curve "B"). Although one would normally expect a higher final population to result from selecting the more distant target year, in fact the population curve for the linear/2060 case tracks substantially above that based on the hyperbolic fertility path to 2080. The reason for

this is that the aggregate of the TFR values for each successive calendar year is considerably greater for the linear path than for the hyperbolic, even though the target year for the latter comes so much later.

One could now go on to examine what happens if both the target year and the sum of the TFR values are the same for two fertility curves. This case is illustrated in *Graph 10b*. The linear and S—curved paths shown here share the same target year of 2060, and the sums of their TFR values are also virtually identical. Nevertheless, the population curve derived from the S—curved path exceeds the curve derived from the linear fertility path not just until the intersection of the paths in the year 2024, but right on until 2076 before it begins to grow more slowly than the other. This phenomenon will be termed the "path effect". Its explanation lies in the momentum of population growth due to the cumulative impact of the age profile on the total population figure. The existence of such path effects further underlines the importance of the pattern of fertility decline for future trends in total population. This conclusion has important connotations for policy-makers, namely that any time lost in reducing fertility levels will lead to an increased overall population figure for many decades, even if that lost time is subsequely made up by a more urgent policy approach.

3.4 The Impact upon World Population Growth of Delays in Reducing Fertility

There are a number of ways in which the decline in fertility rates may be delayed:

- Case 1: For a given pattern of fertility decline, replacement fertility may not be attained until a much later date than the original target.
- Case 2: Even if replacement fertility is indeed attained by the target year, a delay may occur along the way if the path of decline follows the slower S—curve or is linear instead of following the rapid, hyperbolic curve. As shown in the previous section, the result may be an eventual total population which is higher by 3—5 billion.
- Case 3: The lowest level of fertility eventually attained may still exceed the replacement level, meaning that the world population will not reach an upper limit, but will go on growing indefinitely.

These three cases may occur together in a variety of different combinations. Due to space constraints, it will have to suffice here to conclude with a short examination of the case in which replacement fertility is not actually reached. To demonstrate this, a computation has been made (see Table3) based on a final fertility level of 2.17 live births per woman instead of 2.13, with the following result:

Final fertility rate in the year 2080	Population level in the year 2100, in billions
2.13	16.3
2.17	16.7

The difference between the fertility rates is 1.9%, whereas the difference between the corresponding population levels in 2100 is 2.5%. The absolute difference is one of 400 million people. Nevertheless, more important than the absolute difference is the high degree of sensitivity with which population growth responds to small increases in fertility.

If the final fertility rate attained is *below* the replacement fertility level, the world population will still continue growing for a number of decades because of the in-built momentum, then reaching a maximum in the 22nd century before declining slightly thereafter. *Table 4* shows the results emerging from three different final fertility rates (2.0, 2.1 and 2.13), assuming a linear decline in fertility.

3.5 Note on the Precision of World Population Projections to Date

The Population Division of the United Nations' Department of Economic and Social Affairs has been regularly drawing up world population projections since the 1950s. Those projections have in fact proved very reliable. If the projections for the year 2000 which were made in 1958, 1962, 1982 and 1992 are compared, the degree of accuracy achieved is astonishingly good. It is possible to say this today as the world population figure for 2000 is already almost settled at this stage.

Because the projection period is now only 10 years long, the authors' projections for the year 2000 presented here all lie within a relatively narrow range, between 6.1 billion (with 2010 as the target year) and 6.2 billion (with 2080 as the target year). The

UN's projections since 1958, with the exception of the deviating projection made in 1962, equally fit into a range which is hardly any broader. The following table shows the medium variants in each case:

	Projected population
	in the year 2000
1958 UN projection	6.3 billion
1962 UN projection	6.6 billion
1982 UN projection	6.1 billion
1992 UN projection	6.2 billion
The author's projection	6.1-6.2 billion

The precision of projections made in the past does not necessarily mean that they will achieve a correspondingly high degree of precision in the future. Thus it is all the more important to demonstrate the potential scope for variation by portraying alternative scenarios, in the form of "if ..., then ..." projections.

4. The Impact of Alternative Mortality Scenarios upon World Population Growth

4.1 Assumptions on Changes in Life Expectancy

The trend in life expectancy has been computed separately for each individual age cohort within the world population. It is assumed that improvements in health conditions and the overall standard of living will lead to an increase in the average life expectancy of men and women together from 68.5 years for those who are now almost 20 years of age (the 1975 age cohort) to 73.8 years for those born in 2030. No further improvement in life expectancy has been assumed for those born later than the year 2030. Nevertheless, because at least some of the people born in 2030 can be expected to live on beyond the end of the 21st century, the calendar-year life expectancy (according to the period concept conventionally used, rather than the cohort concept used here) will in fact continue to rise, though only slightly, until the end of that century.

The life expectancies assumed by the World Bank and the UN Population Division are more optimistic than those underlying the projections presented here. The World Bank supposes that the average period-concept life expectancy of the two sexes will have increased to 82.3 years by the end of the 21st century. This entails an optimistic assumption that the differential in life expectancies between the industrial and developing countries will by that time have narrowed to just three years (85 years for the industrial countries, 82 years for the developing countries). In 1990, that differential was still 12.4 years (74.3 years in the industrial, 61.9 years in the developing countries).

The author does not share the above optimism. In reality, a more likely presumption is that rapid population growth will create nutrition problems and trigger a number of demographically and politically determined development crises, all of which will prevent health conditions and overall living standards from reaching the levels which would be necessary to attain the long life expectancy of 82 years. For the sake of comparison, it is worth noting that the average current male life expectancy in Germany is 72.2 years, and the female life expectancy 78.7 years.

4.2 The Impact upon World Population Growth of Alternative Assumptions on General Mortality Trends and the Influence of AIDS

Overall life expectancy is a complex measure computed from 200 separately ascertained cohort life expectancies i.e. 100 each for males and females. The probability of mortality (x) is the complementary quantity to the probability of survival (y), i.e. x=1—y. If a change is made to the assumed life expectancy in a population projection, this entails altering 100 male and 100 female age-specific mortality rates, similar to the 31 age-specific fertility rates encountered earlier.

How pronounced, then, are the changes in population projections which result from changed assumptions on mortality? Table 5 and Graph 11 show the results of population projections based on a linear fertility decline with a target year of 2070, with alternative scenarios for a reduction in mortality rates of 1%, 2%, ..., and 10%. Readers will notice that the impact of changes in mortality is comparatively slight relative to changes in fertility: for example, a 5% reduction in mortality in the case illustrated would give rise to a total population of 15.263 billion in the year 2100, as against 15.011 billion with mortality unchanged. A 10% reduction in mortality would lead to a total population of 15.523 billion in the same year.

These findings also illustrate why the influence of AIDS upon world population growth has been estimated to be relatively limited in all demographic surveys to date. For example, the main distinction between the two World Bank projections for Africa contained in *Table 2* is that AIDS was considered as a factor in the later projection (1992/93) whilst it did not play any major part in the earlier projection of 1989/90. The overall difference in Africa's projected population in 2050 is 196 million people. The second projection assumes slightly higher fertility rates than the first, so that under normal circumstances with unchanged mortality a higher rather than a lower population figure would have been expected to result. Consequently, the overall impact of AIDS as projected can be put at between 200 and 250 million people, or less than 10% of the population of the continent in the year 2050.

4.3 The Impact upon World Population Growth of an Increase in Child and Infant Mortality

The computations presented in this section were carried out under the dark shadow cast by an issue which was the focus of discussion at the Deutsches Institut für Ärztliche Mission (Medical Mission Institute) in Tübingen in November 1993. Maurice King, in a controversial article in The Lancet, had put forward the idea that the movement towards "demographic entrapment" faced by the developing countries as their populations grew too large could only be retarded—and therefore had to be retarded by deliberately settling for an increase in child and infant mortality, for the consequence of not doing so would be the destruction of the Earth's ecosystem by overpopulation (8). The proposition harks back to the Thomas Malthus' classic population theory proposed in 1798 (9). This mode of thinking also provides the basis for lifeboat ethics and, taken to its logical conclusion, creates the maxim that to provide aid is immoral (10). Maurice King propounded his ideas in person at the Tübingen conference, and it was the present author's task to respond in a separate paper. That response included a whole series of counter-arguments, some of them ethical but others demographic in their essence. I should like to return to the ethical objections in a separate contribution on another occasion, and at this point will concentrate on the demographic core argument. We shall therefore scrutinize the proposition that an increase in mortality by consciously allowing children in developing countries to die offers the only means of solving the problem of overpopulation on the planet Earth.

Six population projections have been prepared based on the assumption of a linear decline in fertility with the target year for the replacement fertility level set at 2060, in which child and infant mortality is increased by 50%, 100%, ..., 300%. This extreme form of hypothetical experiment produced the results shown in *Table 6* and *Graph 13*:

1. An increase in child and infant mortality even of up to 300% would, assuming a linear decline in fertility with 2060 as the target year for 2.13 live births per woman, still be unable to prevent the continuation of population growth at least until the year 2050, albeit in a less pronounced form. The initial population figure in the base year of 1990 (5.3 billion) would not be reached again until 2135 even if child and infant mortality rose by 300% (Table 6, final column, and Graph 13).

2. In the scenario in which child and infant mortality increases 50%, population growth continues until the year 2100, when it reaches a peak of 12.2 billion. Without any increase in child and infant mortality, the world population in 2100 is projected at 13.8 billion, or 1.6 billion more. Thus, in percentage terms, a 50% increase in child and infant mortality leads to a 12% reduction in the population in 2100.

The conclusion from these calculations is as follows: The grim recommendations made by Maurice King and his Malthusian school are not sufficient to generate a decisive reduction in population growth, nor to resolve population-related problems. Thus the pursuit of such an aim as a matter of deliberate policy would not yield success. While demographically ineffective on the one hand, it would also be quite ghastly in its dehumanizing impact. By resorting to such means, we would cast aside all the objectives we live for. Its inner contradictions push Malthusian policy to the point of absurdity. The fact that such thinking nevertheless has so many supporters is largely a manifestation of a lack of seriousness in analysing demographic problems rather than of ethical incapacity. Consequently, it is a worthwhile exercise to contribute to a clearer insight into the nature of the problems involved by means of rational argument.

5. Summary

International discussion of population issues is chiefly centred around the demographic world population projections published by two United Nations institutions, namely by the World Bank and by the Population Division of the UN Department for Economic and Social Information and Policy Analysis (previously named the Department of International Economic and Social Affairs). These population projections are not a reflection of current prospects, nor are they forecasts or prophecies, but computations which predict exactly what would happen to future population patterns if a particular set of assumptions were met ("if ..., then ..." statements). The "if..." conditions consist of assumptions on the future trends in fertility (as expressed by the total fertility rate, or number of live births per woman) and in mortality (the decrease in mortality or increase in life expectancy). If those assumptions on fertility and mortality should be borne out in reality, then the statements derived from them regarding the future population size will also be correct.

The fertility assumptions underlying the UN population projections are made in the following way. Target years are cited by which time the number of live births per woman (TFR) is assumed to have fallen from 3.3 in the early 1990s to the replacement fertility level. Replacement fertility level refers to the number of live-born children per woman at which the world population will cease to grow in the long term (i.e., some time after the end of the 21st century). At the mortality levels currently assumed, that replacement level of fertility is 2.13 live births per woman. In its medium variant, the World Bank takes 2060 as its target year for replacement fertility. On this optimistic assumption, the world population is projected to grow from 5.3 billion in 1990 to 11.7 billion in 2100. Population growth, on this projection, will come to a stop by 2150, when the world total will be 12.1 billion.

The author's own population projections presented here add a number of additional computed variants to those contained in the UN projections, by including further target years which are both more optimistic than 2060 (i.e., earlier targets such as 2030 or 2040) or more pessimistic (later years) and computing the consequential changes in the world population. Further variations have been included by calculating the impact of different patterns of decline in fertility. For any particular target year, the reduction in the number of live births per woman may, for example, be swift in the initial period but becoming slower over time (i.e., following a hyperbolic curve), or it may be equal each year (i.e., linear). The projections shown here also vary the mortality

assumptions, both to take account of the impact of AIDS and to estimate the consequences for world population growth of deliberately allowing child and infant mortality to rise (i.e., by allowing children in developing countries to die), as advocated by a currently influential Malthusian school of thought.

The most important findings of the alternative population projections presented here are:

- The final population figures computed for the planet Earth of 10.1 billion in the 1. year 2100 and 12.1 billion in 2150 will be exceeded if it does not prove possible by means of development and family policies to achieve a fall in the number of children born per woman in the developing countries from the current level of 3.6 to just 2.5 by 2020-25 and 2.3 by 2025-30. The author is sceptical as to whether this objective can be achieved, for people in the developing countries will find that just two children are insufficient to insure against economic and social risks in countries which lack adequate state provision for unemployment, sickness and old age, especially now that traditional help networks in extended families and local communities are breaking down as economies and societies undergo modernization processes. This could result in a slackening pace of fertility decline in years to come, and the consequence of that in turn would be heavier population growth than has so far been allowed for in the UN's population projections. It is quite possible, and indeed quite likely, that the final world population figure will not settle down at the 12 million, but at the 14 million mark.
- 2. The calculations show that the impact of mortality changes is substantially less than that of fertility changes. For example, AIDS is not expected to have any decisive effect in reducing population growth. The reduction in the eventual population of Africa in the year 2050 resulting from AIDS is estimated at less than 10%.
- 3. Special significance attaches to the future trend in child and infant mortality. Yet even here, variations in mortality still have a relatively low impact on population growth overall. Even if infant and child mortality were to increase by 50%, for example, the world population would still continue to grow up to the year 2100. At that peak level, the total would be only 12% lower than with the initially assumed mortality rates. These alternative mortality scenarios were

calculated in order to demonstrate that any policy following the inhumane recommendations of Malthusian population theorists who advocate deliberately allowing children born in developing countries to die would still not succeed in preventing population growth, quite apart from the ethical unacceptability of such policies.

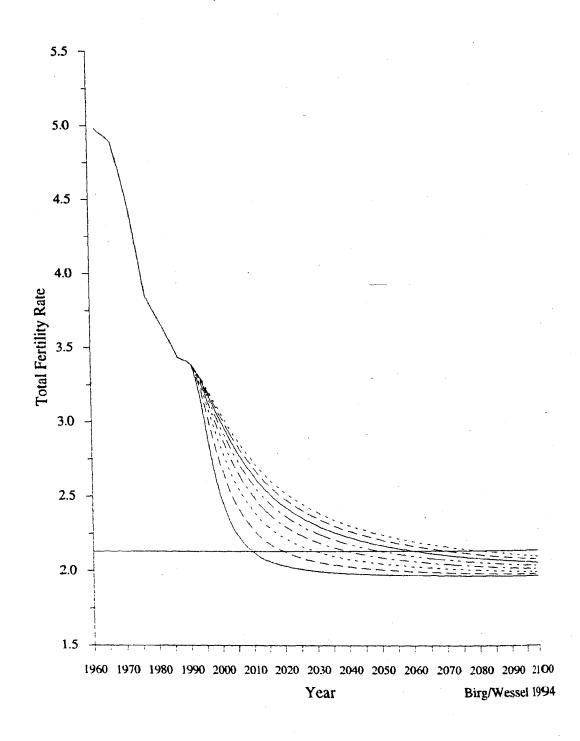
Notes

- (1) E. Bos et al.: World Population Projections, 1992-93 edition, Baltimore and London, 1992. R.A. Bulatao et al.: World Population Projections, 1989-90 edition, Baltimore/London, 1990.
- (2) UN (ed.): World Population Prospects The 1992 Revision, New York, 1993. UN (ed.): World Population Prospects 1990. Population Studies No.120, New York, 1991.
- (3) The initial findings were published in: H.Birg: "Perspektiven des globalen Bevölkerungswachstums Ursachen, Folgen, Handlungskonsequenzen", in: F.Nuscheler and E.Fürlinger (eds): Weniger Menschen durch weniger Armut? Bevölkerungswachstum Globale Krise und ethische Herausforderung, Salzburg/Munich, 1994.
- B. Robey et al.: The Reproductive Revolution: New Survey Findings, Johns Hopkins University Population Program. Population Reports, SeriesM, No.11, Baltimore, October 1992. B.Robey et al.: "Familienplanung in Entwicklungsländern", in: Spektrum der Wissenschaft, February 1994, pp. 32ff.
- (5) W.K. Stevens: "Poor Lands' Success in Cutting Birth Rate Upsets Old Theories", in: The New York Times, January 2, 1994.
- (6) The source of the initial data for 5-year age-groups was: K.C. Zachariah and MyT. Vu: World Population Projections, 1987-88 edition, Baltimore/London, 1988.
- On aggregation effects, see also: W. Lutz and C.Prinz: Scenarios for the World Population in the Next Century: Excessive Growth or Extreme Aging, International Institute for Applied Systems Analysis, WP-91-22, Laxenburg nr. Vienna, 1991. On the aggregation effects shown by regionally disaggregated population projections for Germany, see: H.Birg: "Berechnungen zur langfristigen Bevölkerungsentwicklung in den 343 kreisfreien Städten und Landkreisen der Bundesrepublik Deutschland", in: Vierteljahreshefte zur Wirtschaftsforschung, No.2, 1980, pp. 191—216.

- (8) M. King: "Health is a Sustainable State", in: The Lancet, Sept.15, 1990, pp.664-667. See also: J.Martin: "Would Machiavelli Now be a Better Guide for Doctors than Hippocrates?", in: World Health Forum, WHO, Geneva, Vol.14, 1993, pp. 105—115.
- (9) T.R. Malthus: Essay on the Principle of Population as it Affects the Future Improvement of Society. London, 1798 (Reprint Harmondsworth, 1970).
- (10) H. Birg: "Population Theory and Human Ecology" in: A.Blum and J.—L. Rallu (eds): European Population, Vol.2: Demographic Dynamics, Proceedings of the 1991 European Population Conference, Paris, 1993, pp. 509-525.

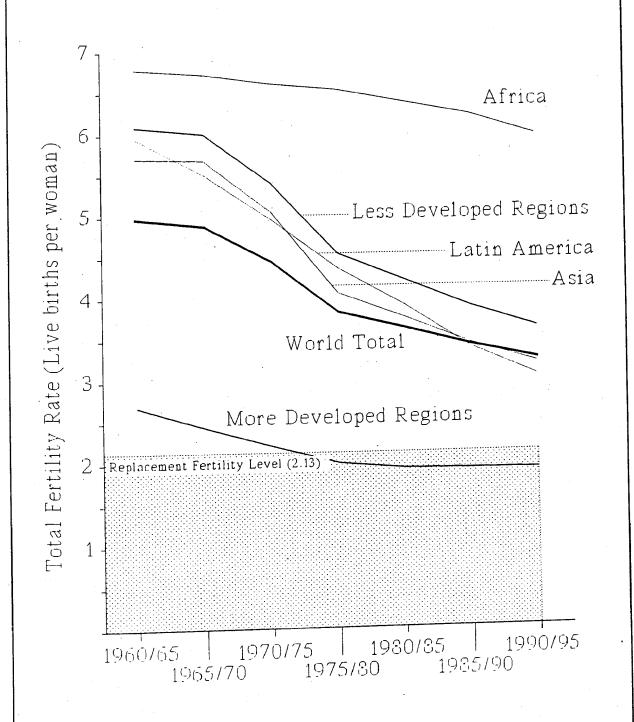
Graph 1a

Decline in the Total Fertility Rate of the World Population from 1962-1990 and Scenarios for the Decline to Replacement Fertility Level (TFR = 2.13) in the Future (Form of Decline: Hyperbolic)



Graph 1b

Decline in the Total Fertility Rate from 1960-65 to 1990-95
by Major Area

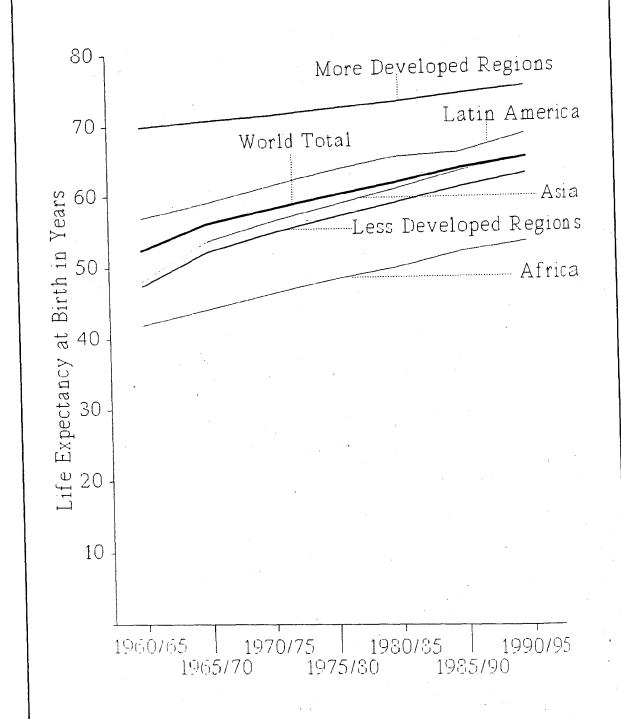


Source of Data: UN (Ed.), World Population Prospects - The 1992 Edition, New York 1993

Birg. 1994

Graph 1c

Increase in Life Expectancy at Birth from 1960-65 to 1990-95 by Major Area

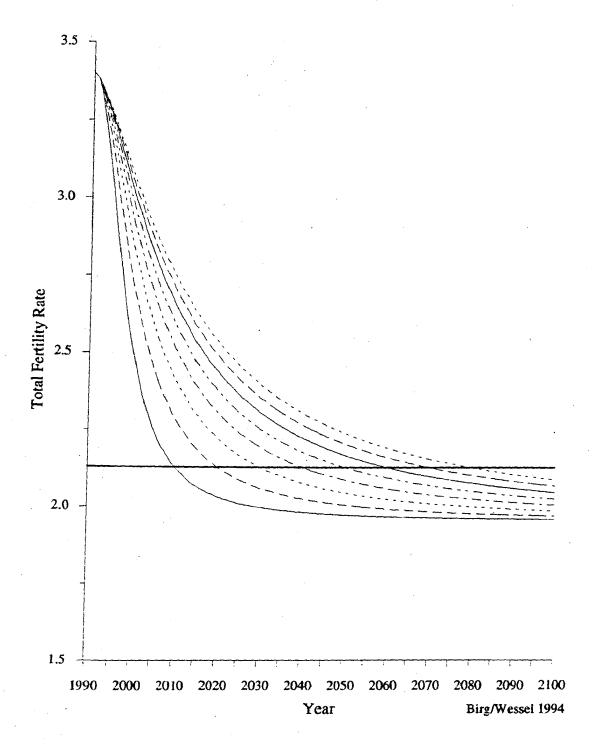


Source of Data: UN (Ed.), World Population Prospects - The 1992 Edition, New York 1993

Graph 2

Decline in the Total Fertility Rate of the World Population to Replacement Fertility Level (TFR = 2.13)

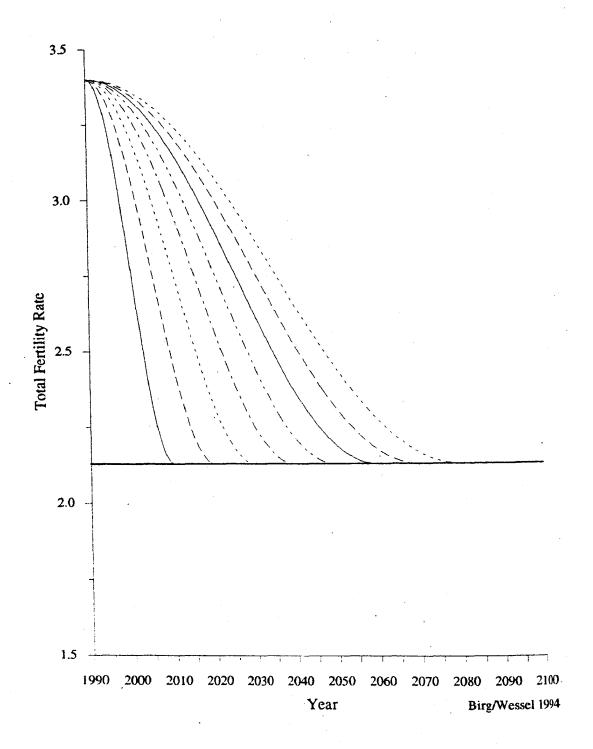
(Form of Decline: Hyperbolic)



Graph 3

Decline in the Total Fertility Rate of the World Population to Replacement Fertility Level (TFR = 2.13)

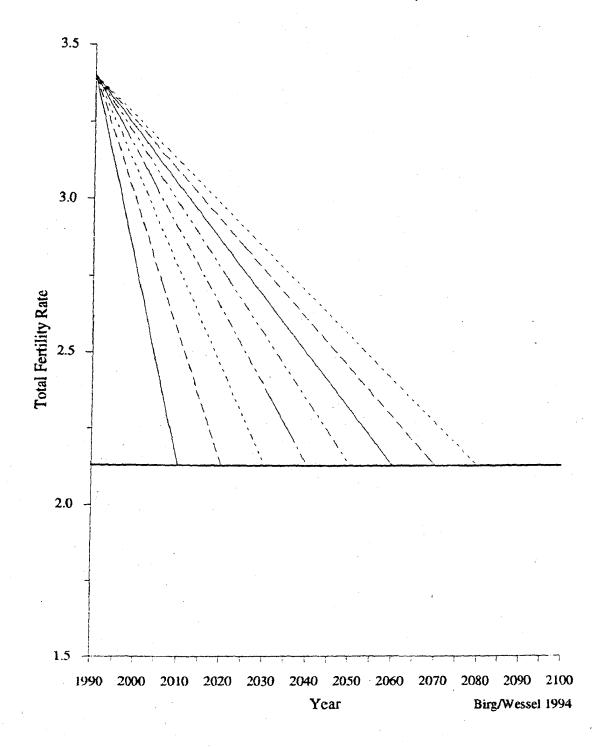
(Form of Decline: S-Shaped)



Graph 4

Decline in the Total Fertility Rate of the World Population to Replacement Fertility Level (TFR = 2.13)

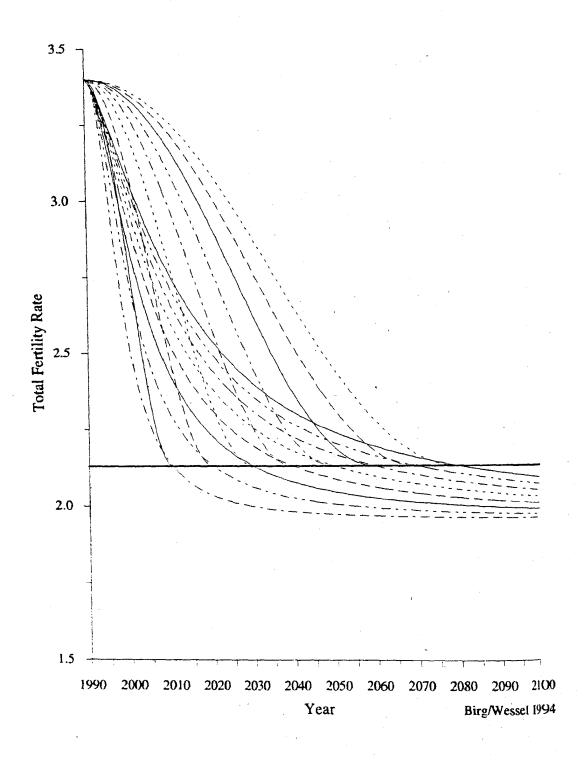
(Form of Decline: Linear)



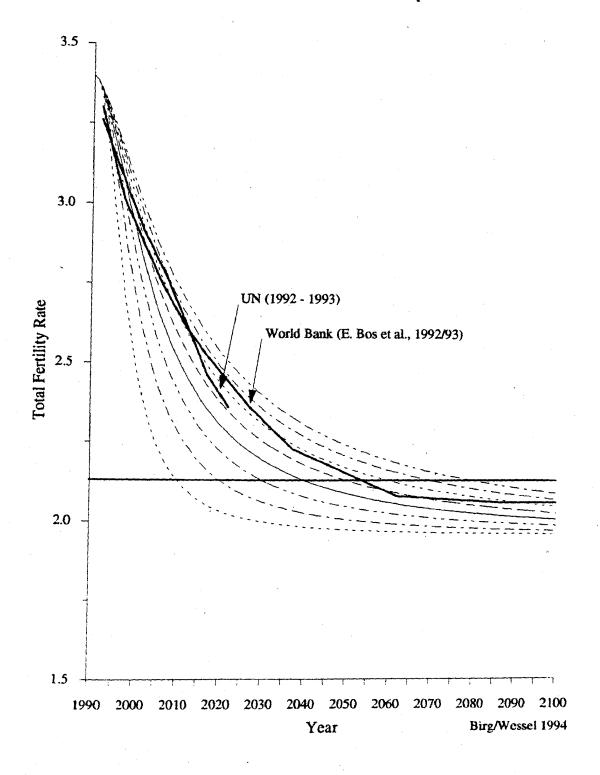
Graph 5

Decline in the Total Fertility Rate of the World Population to Replacement Fertility Level (TFR = 2.13)

(Form of Decline: Hyperbolic and S-Shaped)

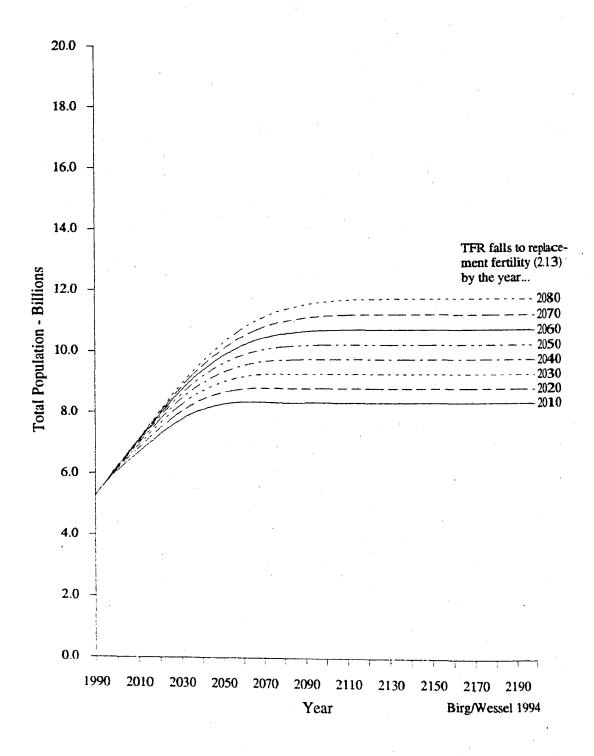


Graph 6
Comparison of Various Assumptions on Fertility Decline for the World Population



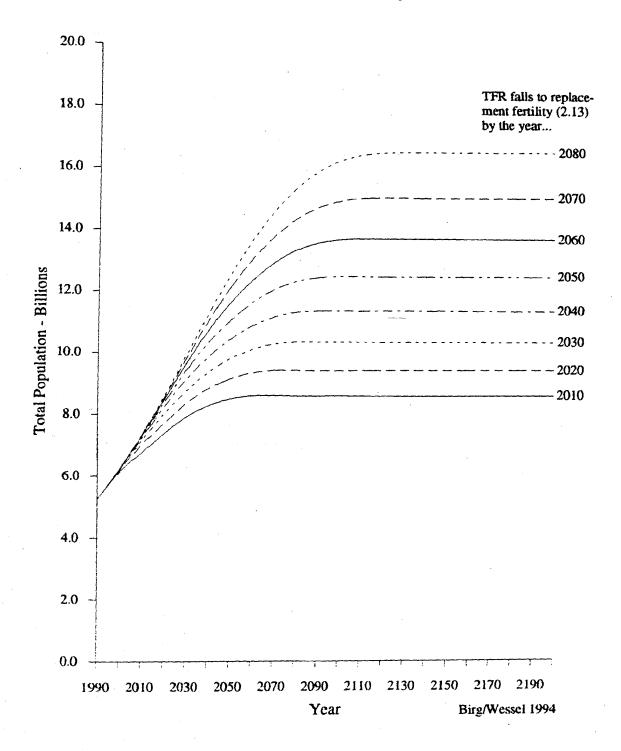
Graph 7

World Population Projections Based on Different Assumptions for the Time Necessary to Achieve Replacement Fertility (Form of Decline: Hyperbolic)



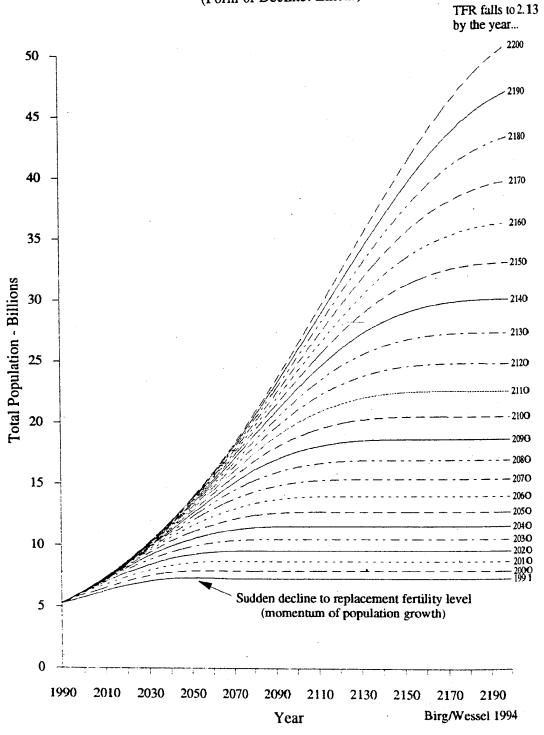
Graph 8

World Population Projections Based on Different Assumptions for the Time Necessary to Achieve Replacement Fertility (Form of Decline: S-Shaped)



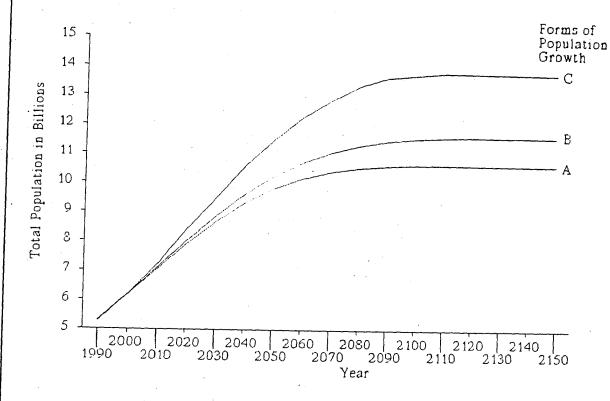
Graph 9

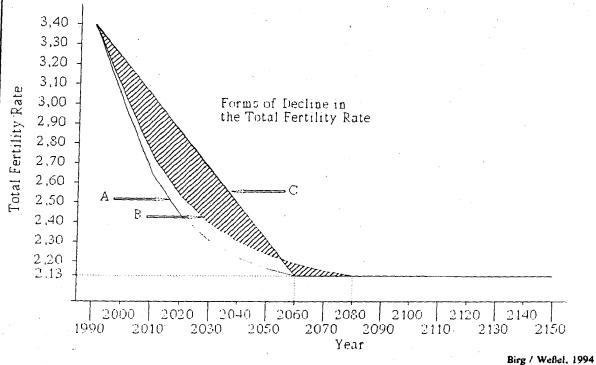
World Population Projections Based on Different Assumptions for the Time Necessary to Achieve Replacement Fertility (Form of Decline: Linear)

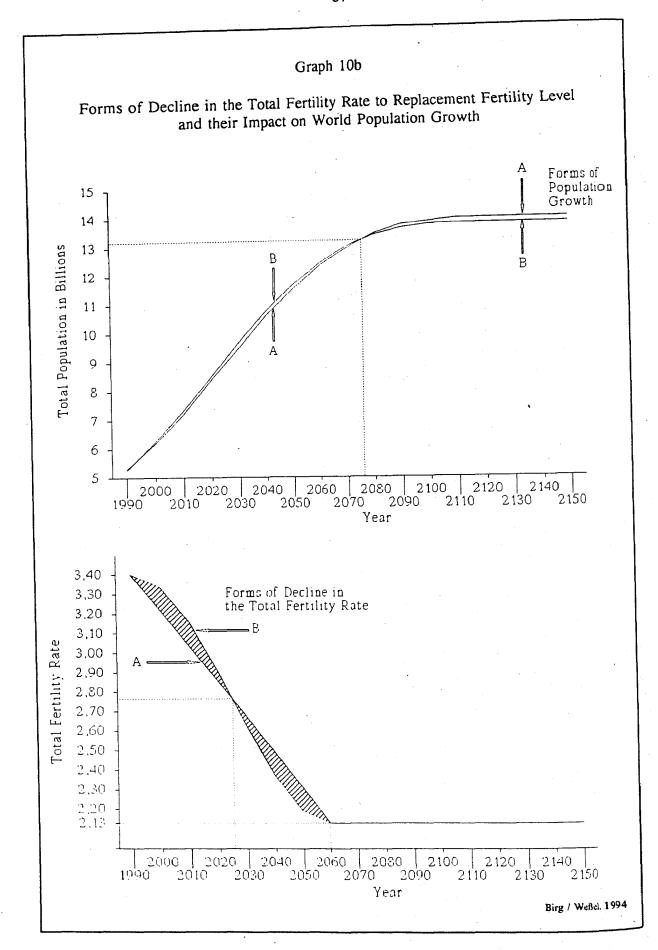


Graph 10a

Forms of Decline in the Total Fertility Rate to Replacement Fertility Level and their Impact on World Population Growth

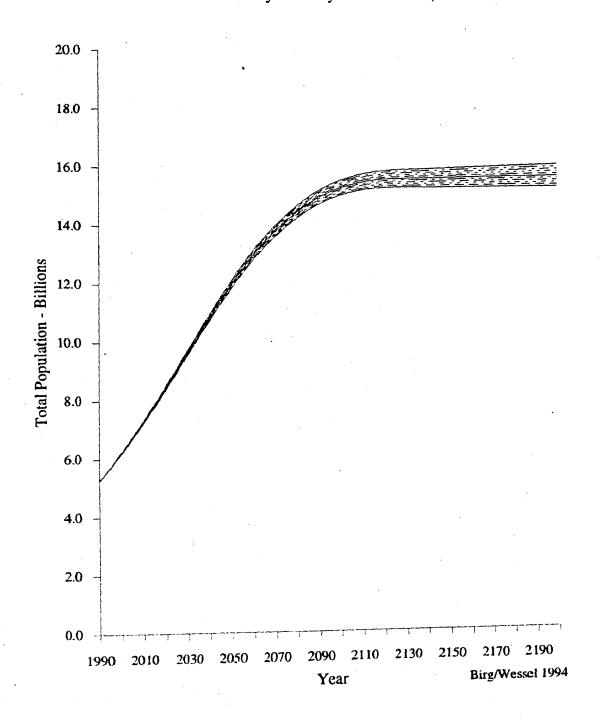






Graph 11

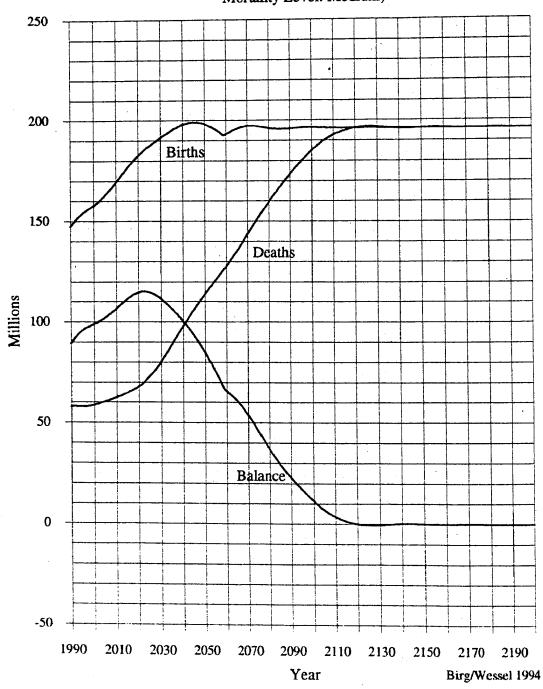
World Population Levels Resulting from
Different Reductions in Mortality
(Mortality Reductions Between 0 and 10 Percent,
Fertility Assumption: Linear Reduction to Replacement
Fertility Level by the Year 2070)



Graph 12

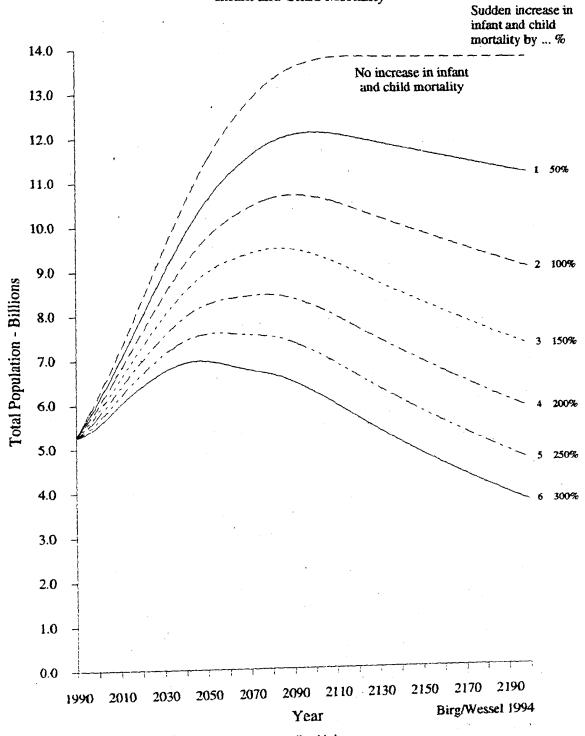
Components of Population Change
World Population Projection No. 2060.A.M
Target Year for Replacement Fertility: 2060
(Form of Fertility Decline: Linear,

Mortality Level: Medium)



Graph 13

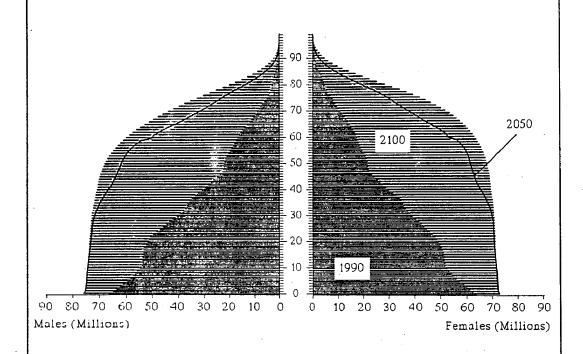
Scenarios of World Population Growth Based on Different Assumptions Concerning an Increase in Infant and Child Mortality



Fertility assumption: Total fertility rate declines from 3.4 live births per woman in 1990 to 2.13 in the year 2060 (linear reduction)

Graph 14

Age Structure of World Population 1990, 2050 and 2100



Population Projection No. 2060.R.M.

Target Year for Replacement Fertility

Level (TFR = 2.13):

Form of Fertility Decline:

Mortality Level:

2060

Hyperbolic

Medium

Absolute Numbers:

1990 5 318 Millions 2050 9 824 Millions

2100 10 674 Millions

Birg / Weßel, 1994

Table 1
The World Population Level in 2150, Based on Different Assumptions as to the Rapidity of the Decline in Fertility (TFR) to the Replacement Level of 2.13 Live Births per Woman

The number of year needed, starting in 1990, for fertility treach replacement	to	assuming dif fertility (TFF	ation in 2150, ferent forms of to the same points per wom	f decline in Final value
level, by the target year of	Target year		Form 2	Form 3
20 vears	2010	8.3	8.6	8.7
20 years 30 years	2020	8.8	9.5	9.5
40 years	2030	9.3	10.4	10.5
50 years	2040	9.7	11.4	11.5
60 years	2050	10.2	12.5	12.7
70 years	2060	10.7	13.7	13.9
80 years	2070	11.2	15.1	15.3
90 years	2080	11.7	16.5	16.8
100 years	2090	12.2	18.2	18.5
110 years	2100	12.7	19.9	20.3
	apid decline in f er time (hyperbo year, after inters	lic function ir	itercepting x-a	ckening xes in the

Form 2: S-shaped decline in three fertility phases:

phase 1 - weak initial decline, but increasingly accelerating;

phase 2 - very pronounced decline;

phase 3 - decline easing off again (sine-function)

Form 3: Equal decline in fertility each year until the target date (linear function)

Table 2
Comparison between the World Bank Population
Projections of 1989/90 and 1992/93

(figures in millions)

	1989/	90 Project	ions	1992/	93 Project	ions
	1990	2050	2150	1990	2050	2150
World	5285	10035	11499	5268	10055	12078
Developing Countries	4074	8716	10186	4053	8623	10610
Industrial Countries	1211	1319	1314	1214	1433	1469
Africa	651	2275	3042	627	2079	2954
America	721	1146	1200	721	1201	1308
of which:						
Latin America	441	814	871	441	839	935
North America	280	332	329	280	362	373
Asia	3100	5728	6367	3103	5811	6817
Europe and	787	843	846	790	922	954
former USSR						
Oceania	27	42	45	27	43	46

Compiled from: (a) R. A. Bulatao et al.: World Population Projections 1989 - 90 Edition, Baltimore and London, 1990; (b) E. Bos et al.: World Population Projections 1992 - 93 Edition, Baltimore and London, 1992.

Table 3
World Population Growth Assuming a Linear
Decline in Fertility up to 2080 (in Billions)

	final fertility value in the year 2080 1)					
•	TFR = 2.13 TFR = 2.17					
1990	5.3	5.3				
2050	12.2	12.3				
2100	16.3	16.7				
2150	16.8	17.8				
2200	16.8	18.4				

assuming constant fertility thereafter,
 and the medium mortality variant

Table 4

The Impact of Delays in the Decline in Fertility to the Replacement Level (TFR = 2.13), or to Just Under Replacement Level (TFR = 2.0 or 2.1)

Length of t	ime needed decline	World population in 2150, in billions assuming final fertility values of				
		TFR = 2.0	TFR = 2.1	TFR = 2.13		
50 years	(= 2040)	8.9	10.9	11.5		
60 years	(= 2050)	10.0	12.0	12.7		
70 years	(= 2060)	11.1	13.2	13.9		
80 years	(= 2070)	12.4	14.6	15.3		
90 years	(= 2080)	13.8	16.1	16.8		
100 years	(= 2090)	15.4	17.7	18.5		
110 years	(= 2100)	17.1	19.6	20.3		
120 years	(= 2110)	19.0	21.5	22.3		
130 years	(= 2120)	21.0	23.5	24.3		
140 years	(= 2130)	23.1	25.7	26.5		
150 years	(= 2140)	25.2	27.8	28.6		
Assumption	: Linear fertilit	y decline, mediu	m mortality lev	vel .		

Table 5
The Influence of Alternative Assumptions on the Outcome of World Population Projections

. •					Reductio	Reduction in Mortality Rates			ord t opalation trojections	Silo	
	%0	1%	2%	3%	4%	2%	%9	7%	8%	%6	10%
Year					populat	population figures in 1000	1000				
19 <u>%</u>	5274612	5274612	5274612	5274612	5274612	5274612	5274612	5274612	5274612	5274612	5274612
2000	6226719	6231554	6236404	6241268	6246147	6251040	6255948	6260871	6265809	6270763	1823229
2010	7263292	7271982	7280707	7289465	7298259	7307089	7315955	7324858	7333798	7342775	7351701
2020	8406721	8419432	8432197	8445016	8457890	8470820	8483807	8496852	8509955	8523118	8536341
2030	9614606	9631684	9648135	0909996	9683361	9700738	9718193	9735726	9753340	9771035	9788813
2040	10785893	10807722	10829651	10851679	10873810	10896045	10918385	10940832	10963388	10986053	11008831
2050	11876315	11903078	11929969	11956991	11984145	12011434	12038859	12066424	12094129	12121978	12149973
2060	12845864	12877524	12909342	12941320	12973462	13005769	13038245	13070891	13103711	13136707	13169883
2070	13634925	13671478	13708224	13745164	13782302	13819640	13857182	13894930	13932889	13971060	14009448
2080		14292201	14333666	14375366	14417304	14459484	14501911	14544586	14587515	14630702	14674151
2080		14759771	14805676	14851853	14898304	14945035	14992049	15039352	15086948	15134842	15183038
2100	15011333	15061070	15111111	15161460	15212123	15263103	15314407	15366039	15418005	15470310	15522959
2110		15233165	15286829	15340837	15395196	15449910	15504985	15560428	15616243	15672439	15729020
2120		15309742	15366489	15423613	15481118	15539011	15597299	15655986	15115081	15774590	15834519
2130		15326782	15386116	15445853	15505999	15566560	15627543	15688955	15750803	15813094	15875837
2140	_	15323942	15385477	15447435	15509822	15572646	15635914	15699633	15763810	15828453	15893570
2150	15261433	15324618	15388235	15452292	15516794	15581750	15647167	15713051	15779411	15846255	15913591
2160		15328173	15393962	15460208	15526918	15594098	15661757	15729901	15798539	15867680	15937330
2170		15328820	15396776	15465209	15534126	15603533	15673439	15743851	15814777	15886227	15958208
2180		15330511	15400606	15471197	15542289	15613893	15686014	15758661	15831843	15905567	15979844
212		15332407	15404666	15477440	15550736	15624563	15698928	15773840	15849308	15925340	16001945
2200	15259941	15333827	15408242	15483192	15558686	15634731	15711336	15788510	15866261	15944598	16023531
7	•	•							ı		

Fertility assumptions: Target year of 2070 for replacement fertility, linear decline

Table 6
World Population Level (in 1000) Assuming a Sudden
Increase in Infant and Child Mortality (Malthusian Variant)

Variant	ı	I (+50 %)	1	n	(+ 100 %)	, 1	. 11	I (+ 150 %)	
	Males	Females	Total	Males	Females	Total	Males	Females	Total
Age 1990	2657196	2617416	5274612	2657196	2617416	5274612	2657196	2617416	5274612
2000	3075113	3021870	6096983	3012240	2965240	5977480	2951934	2910802	5862736
2010	3528683	3484844	7013528	3412245	3383319	6795563	3300774	3285786	6586560
2020	4001097	3980626	7981722	3815305	3819341	7634646	3639780	3666163	7305943
2030	4475424	4486102	8961526	4209673	4254091	8463764	3960356	4034935	7995291
2040	4903341	4947370	9850711	4552074	4638625	9190700	4224776	4348752	8573528
2050	5260817	5334729	1	4819840	4943123	9762963	4411881	4577851	8989732
2060	5533801		11168435	5008761	5161504		4526382	4722899	9249281
2070	5741467		11609856	5144101		10465741	4599561	4818326	9417887
2080	5888649		11929532	5232826		10666724	4640317	4879754	9520071
2090	5964393		12103056	5257833		10736401	4625211	4881153	9506365
2100	5983890		12158151	5231579		10696219	4563859	4827836	9391695
2110	5961549		12123122	5168615		10576760	4471056	4737903	9208959
	5915623		12034186	5085006		10409712	4360798	4624743	8985542
2120	5863355		11927845	4996854		10229203	4248050	4505087	8753137
2130	ł		11825382	4911857		10054579	4139716	4389653	8529369
214 0	5813340		11726641	4829022	5056325	9885347	4034726	4278620	8313346
2150	5764614		- 1					4169210	8100767
2160	5715150		11626018	4746601	4970022	9716623 9551574	3931 <i>5</i> 57 3831409	4062914	7894322
2170	5666624		1	4666027	4885547	- 1	3733809		
2180	5618511		11429398	4586823	4802695	9389518		3959484	7693294
2190	5570648		11332007	4508828	4721008	9229836	3638583	3858484	7497067
2200	5523303	3/12363	11235686	4432252	4640819	9073071	3545862	3760152	7306015
Variant		V (+ 200 %			(+ 250 %			I (+ 300 %)	
Age	Males	Females	Total	Males	Females	Total	Males	Females	Total
1990	2657196	2617416	5274612	2657196	2617416	5274612	2657196	2617416	5274612
2000	2894155	2858522	5752677	2838862	2808367	5647229	2786016	2760304	5546320
2010	3194164	3192165	6386329	3092310	3102378	6194688	2995109	3016346	6011456
2020	3474095	3520787	6994882	3317837	3382921	6700757	3170610	3252279	6422889
2030	3726688	3828093	7554781	3507914	3633043	7140958	3303311	3449282	6752593
2040	3920102	4076808	7996910	3636776	3821893	7458669	3373584	3583149	6956733
2050	4034835	4237408	8272244	3686717	3920366	7607083	3365652	3625370	6991022
2060	4083645		e annacol	2/22202	2040400	2610006	2205001	0.500.000	
	1	4316624	8400269	3677727	3940608	7618335	3305981	3592902	6898884
2070	4103713	4355373	8459085	3652710	3929903	7582613	3242983	3539228	6782211
2080	4103713 4105668	4355373 4374305	8459085 8479973	3652710 3623847	3929903 3913707	7582613 7537554	3242983 3190216	3539228 3494389	6782211 6684605
2080 2090	4103713 4105668 4059584	4355373 4374305 4341035	8459085 8479973 8400620	3652710 3623847 3554600	3929903 3913707 3853253	7582613 7537554 7407853	3242983 3190216 3104453	3539228 3494389 3413239	6782211 6684605 6517691
2080 2090 2100	4103713 4105668 4059584 3972123	4355373 4374305 4341035 4257041	8459085 8479973 8400620 8229164	3652710 3623847 3554600 3448562	3929903 3913707 3853253 3746033	7582613 7537554 7407853 7194594	3242983 3190216 3104453 2986101	3539228 3494389 3413239 3289131	6782211 6684605 6517691 6275232
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